

## Lecture 8

# Transportation Problem (TP) and Transshipment Problem

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# Unbalanced Problems

- **If (Total Supply) > (Total Demand),**
  - then for Excess supply is assumed to go to the inventory and costs nothing for shipping.
  - Dummy destination column is added, whose demand equals the difference between the total supply and total demand and zero transportation cost
- **If (Total Supply) < (Total Demand),**
  - ***a dummy source is created, whose supply equals the difference.***
  - **All unit shipping costs into a dummy destination or out of a dummy source are 0.**

## Example 1: Balanced Problem

		DESTINATIONS				Supply
		D <sub>1</sub>	D <sub>2</sub>	D <sub>3</sub>	D <sub>4</sub>	
Sources	S <sub>1</sub>	50	75	30	45	12
	S <sub>2</sub>	65	80	40	60	17
	S <sub>3</sub>	40	70	50	55	11
Demand		10	10	10	10	

## Example 2: Unbalanced Problem

	Destination				Supply
	D1	D2	D3	D4	
S1	50	75	35	75	12
S2	65	80	60	65	17
S3	40	70	45	55	11
(Dummy)	?	?	?	?	??
Min Demand	0	0	0	0	
Max Demand	15	10	15	10	

	Destination				Supply
	D1	D2	D3	D4	
S1	50	75	35	75	12
S2	65	80	60	65	17
S3	40	70	45	55	11
<b>(Dummy)</b>	<b>0</b>	<b>0</b>	<b>0</b>	<b>0</b>	<b>10</b>
<b>Min Demand</b>	0	0	0	0	
<b>Max Demand</b>	15	10	15	10	

**Total Supply = 40**

**Total Max Demand = 50**

**Add Dummy Source with costs =0 to all real Destination and  
Supply =50-40=10**

	Destination					Supply
	D1	D2	D3	D4	Dummy	
S1	50	75	35	75	?	12
S2	65	80	60	65	?	17
S3	40	70	45	55	?	11
<b>Min Demand</b>	0	0	0	0		
<b>Max Demand</b>	7	13	5	10	?	

**Total Supply = 40**

**Total Max Demand = 35**

	Destination					Supply
	D1	D2	D3	D4	Dummy	
S1	50	75	35	75	0	12
S2	65	80	60	65	0	17
S3	40	70	45	55	0	11
<b>Min Demand</b>	0	0	0	0		
<b>Max Demand</b>	7	13	5	10	5	

**Total Supply = 40**

**Total Max Demand = 35**

**Add Dummy Destination with costs =0 from all real Sources  
and Demand =40-35=5**

## Example 2: Unbalanced Problem

	Destination				Supply
	D1	D2	D3	D4	
S1	50	75	35	75	12
S2	65	--	60	65	17
S3	40	70	45	55	11
(Dummy)	??	??	??	??	??
<b>Min Demand</b>	15	5	0	10	
<b>Max Demand</b>	15	13	10	$\infty$	



## Example 2: Unbalanced Problem

	Destination				Supply
	D1	D2	D3	D4	
S1	50	75	35	75	12
S2	65	<b>M</b>	60	65	17
S3	40	70	45	55	11
<b>(Dummy)</b>	<b>??</b>	<b>??</b>	<b>??</b>	<b>??</b>	<b>??</b>
<b>Min Demand</b>	15	5	0	10	= total supply – total min demand for all other Destinations =40-20
<b>Max Demand</b>	15	13	10	$\infty$ = 20	

## Example 2: Unbalanced Problem

	Destination						Supply
	D1	D21	D22	D3	D41	D42	
S1	50	75	75	35	20	20	12
S2	65	M	M	60	50	50	17
S3	40	70	70	45	40	40	11
<b>(Dummy)</b>	<b>M</b>	<b>M</b>	<b>0</b>	<b>0</b>	<b>M</b>	<b>0</b>	<b>18</b>
Min Demand	15	5	0	0	10	0	
Max Demand	15	5	8	10	10	10	

# Transshipment Problem

special case of Integer Linear  
Programming

# Transshipment Problems

- ✓ A transportation problem allows only shipments that go directly from supply points to demand points.
- ✓ Transshipment problems are transportation problems in which a shipment may move through intermediate nodes (Junction nodes) before reaching a particular destination node.
- ✓ Fortunately, the optimal solution to a transshipment problem can be found by converting it to transportation problems and solved by transportation Algorithm.

**The following steps describe how the optimal solution to a transshipment problem can be found by solving a transportation problem.**

Let  $s = \text{total Number of units in the system} = \max(\text{Total Supply}, \text{Total Dem})$

**Step1.** If necessary, add a dummy destination or dummy source to balance the problem.

**Step2.** construct a transportation tableau as follows:

- ✓ A row in the tableau will be needed for each source and junction point.
- ✓ A column will be needed for each destination and junction point
- ✓ Each supply point will have a supply equal to its original supply, and each demand point will have a demand equals to its original demand.
- ✓ each Junction point will have  
supply = its original supply + S, and  
demand = its original demand + S

Each location in the Figure will be classified as one of the following cases

*Let  $s = \text{total available units in the system} = \max(\text{Total Supply}, \text{Total Demand})$*

**1. Pure source:** is a point that can send goods to another point but can not receive goods from any other point

from the figure: it is a source has supply and all arrows out from it, or there are arrows in and out, but it is the only source in the system.  $\rightarrow\rightarrow$  its supply equals to its original supply

**2. Pure Destination:** is a point that can receive goods from other points but cannot send goods to any other point.

from the figure it is Destination has Demand and all arrows in, or there are arrows in and out but it is the only Destination in the system.  $\rightarrow\rightarrow$  Its demand equals to its original demand

**3- Pure Junction** (transshipment point ): is a point that can both receive goods from other points and send goods to other points

From the figure: it is neither source nor Destination and it has arrows in and out so units can pass through it.

Each Junction point will be considered as source have a supply equals to  $s$  and a destination wants demand equals to  $s$ .

**4- Combined source and junction:** if it is a source and it has arrows in and out

it will be modelled as a Source with  $\text{supply} = \text{it's original supply} + s$  and a destination with  $\text{demand} = s$

**5- Combined destination and junction:** if it is a destination and it has arrows in and out

it will be modelled as a source with  $\text{supply} = s$  and destination with  $\text{demand} = \text{its original demand} + s$

**Total Supply = 25 + 15 + 50 = 90**

**Total Demand = 70 + 20 = 90**

**→ Balanced Problem**

**Total Units in the System = S = 90**

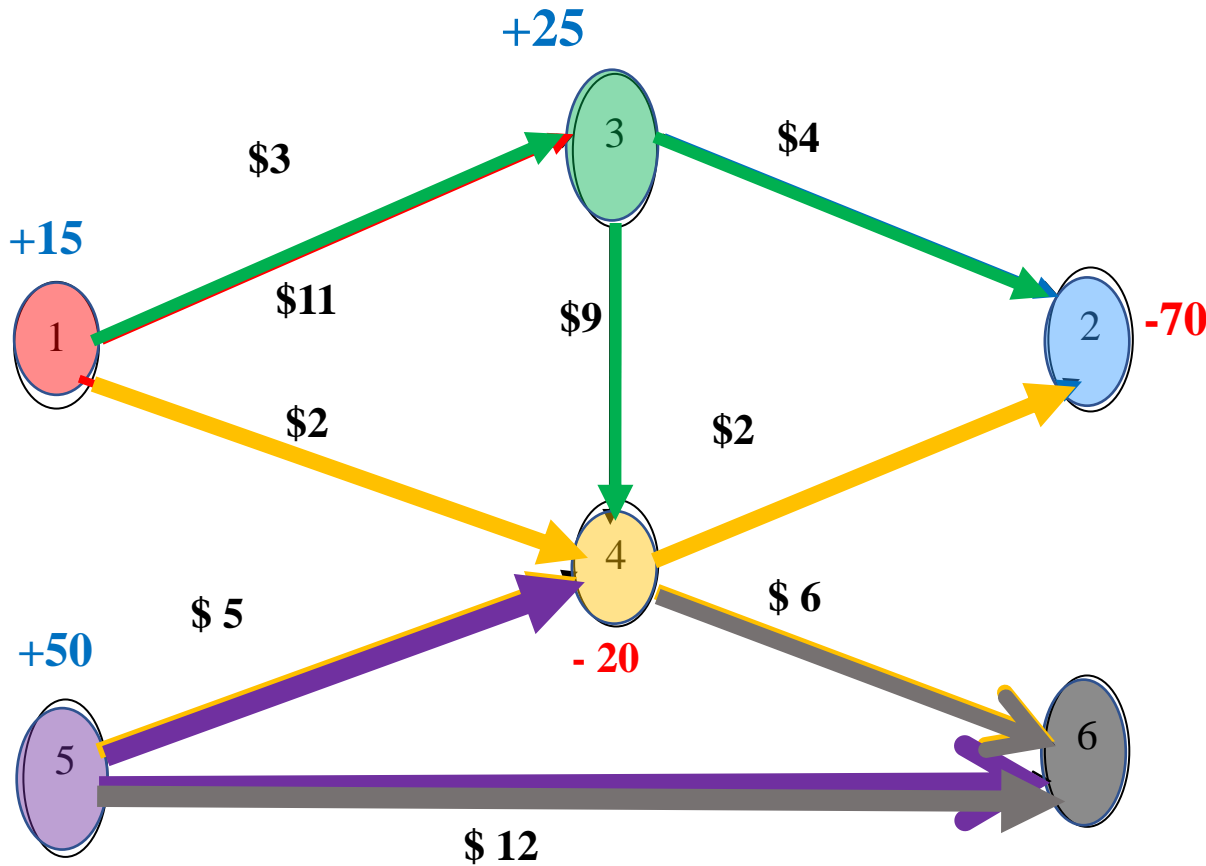
**Location 1:** Pure source with supply=15

**Location 2:** Pure Dest with Demand =70

**Location 3:** source + junction  
 Source Supply = S  
 Dest Demand = S  
 with Supply = 90 + 25 = 115 , Dem = 90

**Location 4:** Dest + junction  
 Source Supply = 90  
 Dest Demand = 90  
 with Supply = 90, Dem = 90 + 20 = 110

**Location 5:** pure source supply =50





	Dest 2	Dest3	Dest4	Supply
Source1	M	3	2	15
Source3	4	0	9	115
Source4	2	M	0	90
Source5	M	M	5	50
Demand	70	90	110	

**Location 1:** Pure source with supply=15

**Location 2:** Pure Dest with Demand =70

**Location 3:** source + junction

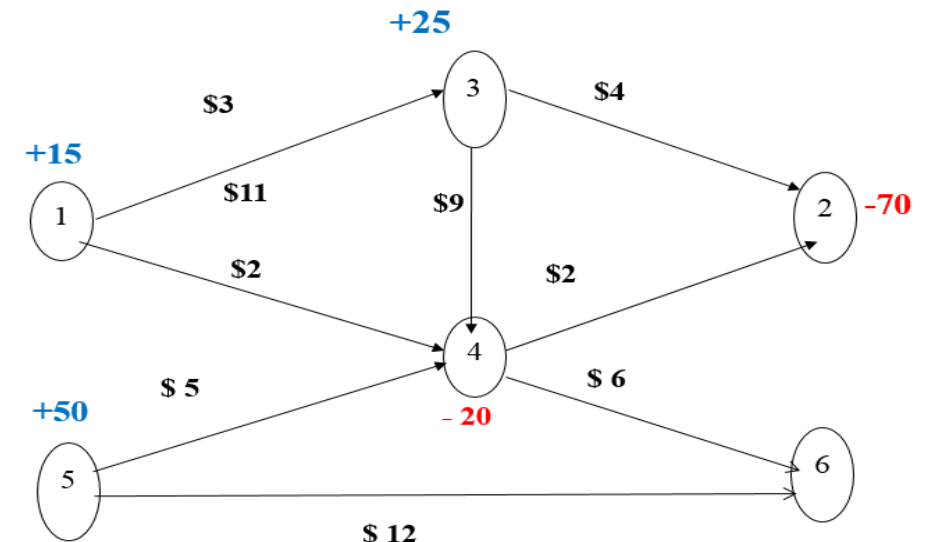
with *Supply* = 90 + 25 = 115, *Dem* = 90

**Location 4:** Dest + junction

with *Supply* = 90, *Dem* = 90 + 20 = 110

**Location 5:** pure source with supply =50

**Location 6: Nothing**

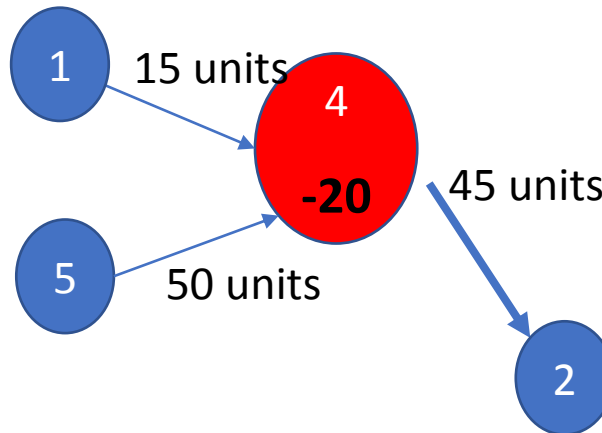


**Shipments from a point to itself will cost zero.**

	Dest 2	Dest3	Dest4	Supply	$u_i$
Source1	11 (+)	3 (+)	2 <b>15</b>	15	2
Source3	4 <b>25</b>	0 <b>90</b>	9 (+)	115	2
Source4	2 <b>45</b>	M (+)	0 <b>45</b>	90	0
Source5	11 (+)	M (+)	5 <b>50</b>	50	5
Demand	70	90	110		
$V_j$	2	-2	0		

Location 3 to itself = 90 unit  
 this mean that 90 units didn't use Location 3 as a junction → so 0 units use it as a junction.

Location 4 to itself = 45  
 This mean that 45 units didn't use Location 4 as a junction → so only 90-45 use it as a junction.



End The  
Operations Research  
Course

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وبالتوفيق للجميع ان شاء الله

و. صفاء السيد أمين

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