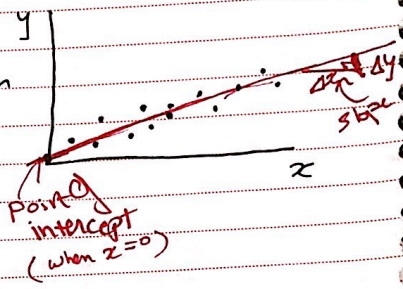


• We try to teach Computer to find the best line that pass through these points

• a line is represented by slope and point of intercept (intersection with the y axis)



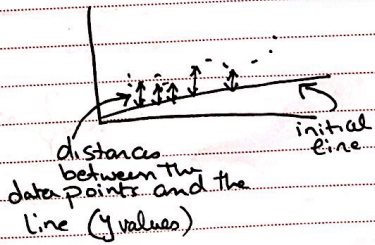
equation of straight line

$$y = ax + b$$

• We start by suggesting any random values for a and b  
The main idea is that we keep enhancing the values of a and b iteratively until reach the best values (the values that make the line the closest to the given data points) (optimization)

• therefore each iteration we calculate the distance between the suggested line and the points and try to minimize that distance

• to get the distance between the points and the line suggested we substitute in the equation of the suggested line



$$\text{Prediction} = a_1 x + b_1$$

Such that  $a_1$  and  $b_1$  are the initial random suggested values for the line

- We are calculating the error between the points on the suggested line and the data points (تقريب مباشر في معادلة الخط)

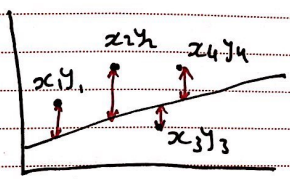
mean square error

predicted y (point on the line)

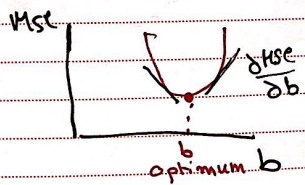
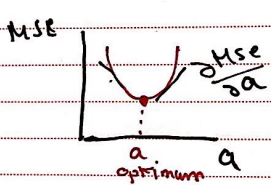
$$MSE = \frac{1}{2n} \left( (y_1 - (ax_1 + b))^2 + (y_2 - (ax_2 + b))^2 + \dots + (y_n - (ax_n + b))^2 \right)$$

↑  
number of data points

- We want to minimize the red lines (distances between each data point and its corresponding point on the line)



- In other words, we want to find the minimum value of the MSE i.e. find the best values of a and b that give us the min value of MSE



So we consider MSE to be function of a and function of b and through partial derivatives we find the best (optimum) value of a and of b

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$$\frac{\partial \text{Mse}}{\partial a} = \frac{1}{2n} \left[ 2(y_1 - (ax_1 + b))(-x_1) + 2(y_2 - (ax_2 + b))(-x_2) + \dots + 2(y_m - (ax_m + b))(-x_m) \right]$$

Solving the above equation

$$\begin{aligned} \therefore \frac{\partial \text{Mse}}{\partial a} &= -\frac{1}{n} \left( \text{all } y_{\text{data}} - \text{all } y_{\text{prediction}} \right) \left( \text{all } x_{\text{data}} \right) \\ &= \frac{1}{n} \left( \text{all } y_{\text{prediction}} - \text{all } y_{\text{data}} \right) \left( \text{all } x_{\text{data}} \right) \end{aligned}$$

Similarly  $\frac{\partial \text{Mse}}{\partial b}$  is calculated in the same manner and equal =  $(\text{all } y_{\text{prediction}} - \text{all } y_{\text{data}})$

$$a_{\text{new}} = a_{\text{old}} - \text{Lr} \left( \frac{\partial \text{Mse}}{\partial a} \right)_{\text{at } a_{\text{old}}}$$

$$b_{\text{new}} = b_{\text{old}} - \text{Lr} \left( \frac{\partial \text{Mse}}{\partial b} \right)_{\text{at } b_{\text{old}}}$$